

**COLLEGE OF ARTS AND SCIENCES** 

# SYLLABUS: STAT 7303 STATISTICAL THEORY II SPRING 2023

# **Course overview**

#### Instructor

Instructor: Mario Peruggia

Email address: peruggia@stat.osu.edu

Phone number: 614-292-0963

Office hours: Virtual Hours via CarmenZoom: Tuesday 1:30-2:30 pm and Friday 3:00-4:00 pm.

The instructor will also be available to answer any questions by appointment.

Office Location: 205A Cockins Hall

#### Grader

Zhizhen Zhao

Email address: zhao.3053@osu.edu

# **Course description**

This course explores basic elements of decision theory and Bayesian inference. During the semester we will cover the following core topics:

- Bayesian Expected Loss, Frequentist Risk, Bayes Risk
- Decision Principles (Bayesian, Frequentist, Likelihood)
- Foundations (Likelihood Principle, Conditionality Principle)
- Loss Functions
- Prior Distributions (Subjective, Noninformative, Improper, Empirical, Hierarchical)
- Posterior Distributions
- Bayes Inference (Estimation, Credible Sets, Hypothesis Testing, prediction)

- Empirical Bayes Analysis
- Hierarchical Bayes Models
- Bayesian Calculation
- Bayesian Model Assessment and Robustness

# **Course learning outcomes**

By the end of this course, students should successfully be able to:

- Understand central elements of decision theory
- Compute Bayes risk and frequentist risk and derive Bayes rules
- Understand important statistical principles that motivate various modes of inference
- Build realistic Bayesian models and specify appropriate prior distributions using a variety of approaches
- Perform fundamental Bayesian inferential tasks
- Assess and validate the assumptions underlying empirical Bayes and hierarchical Bayes models

A more detailed, tentative course plan is provided at the end of this document.

#### **Course materials**

#### Required

The required textbook for this course is:

Berger, J.O. (1985), "Statistical Decision Theory and Bayesian Analysis," second edition, New York, NY: Springer.

The eBook is freely available for download from the OSU library website: https://library.ohio-state.edu/record=b8694733

#### **Optional materials**

Some topics covered in the course will be based on material presented in additional books and articles. Appropriate references will be provided as needed.

## **Course technology**

The course is scheduled to be offered in person. Office hours will be held via Zoom sessions. To be able to attend office hours and to complete some course requirements (including the homework), certain technical skills for online courses will be relevant. These skills should already be familiar to most students.

For help with your password, university e-mail, Carmen, or any other technology issues, questions, or requests, contact the OSU IT Service Desk. Standard support hours are available at <a href="https://ocio.osu.edu/help/hours">https://ocio.osu.edu/help/hours</a>, and support for urgent issues is available 24x7.

• Self-Service and Chat support: http://ocio.osu.edu/selfservice

Phone: 614-688-HELP (4357)

Email: 8help@osu.eduTDD: 614-688-8743

#### Baseline technical skills necessary for online courses

Basic computer and web-browsing skills

Navigating Carmen

#### Technology skills necessary for this specific course

- CarmenZoom
- Ability to upload assignments to Carmen (Word or PDF format)

#### **Necessary equipment**

- Computer: current Mac (OS X) or PC (Windows 10+) with high-speed internet connection
- Webcam: built-in or external webcam, fully installed
- Microphone: built-in laptop or tablet mic or external microphone

#### **Necessary software**

- Some components of this class may require you to use the statistical software package called R (The R Project for Statistical Computing; <a href="http://www.r-project.org/">http://www.r-project.org/</a>). This software package is available as Free Software.
  - You can download R for Windows, Mac, and Linux, from the CRAN archive at https://cran.r-project.org.
  - An in-depth introduction to R is available at <a href="http://cran.r-project.org/doc/manuals/R-intro.pdf">http://cran.r-project.org/doc/manuals/R-intro.pdf</a>
  - Hands-on tutorials are available in the Swirl system, which you can learn about at <a href="http://swirlstats.com/">http://swirlstats.com/</a>. In particular, "R Programming: The basics of programming in R" is an appropriate first tutorial for students who have never used R.
- An easier to use interface to R is available in the software package RStudio. This package
  is available for Windows, Mac, and Linux and can be downloaded for free from
  <a href="http://rstudio.org">http://rstudio.org</a>. Note that RStudio requires R to be installed.
- Microsoft Office 365 ProPlus. All Ohio State students are now eligible for free Microsoft Office 365 ProPlus through Microsoft's Student Advantage program. Each student can

install Office on five PCs or Macs, five tablets (Windows, iPad® and Android™) and five phones.

- Students are able to access Word, Excel, PowerPoint, Outlook and other programs, depending on platform. Users will also receive 1 TB of OneDrive for Business storage.
- Office 365 is installed within your BuckeyeMail account. Full instructions for downloading and installation can be found <a href="https://ocio.osu.edu/kb04733">https://ocio.osu.edu/kb04733</a>.

# **Course delivery**

The course is scheduled to be offered in person. We will meet MWF 1:50-2:45 in Caldwell Laboratory 109.

Zoom links for the course office hours will be listed on Carmen.

# **Grading and faculty response**

#### **Grades**

Assignment or category	Percentage
Homework	20%
Midterm Exam I	20%
Midterm Exam II	20%
Final Exam	40%
Total	100

# **Assignment information**

Grades will be recorded on the class website.

Homework: There will be regular homework assignments (11 are scheduled as of now). Homework must be uploaded to Carmen by the posted deadline on the day it is due. Homework is **not** accepted by email. Late homework is not accepted, but the lowest homework score will be dropped. You are encouraged to work together on the homework, but do not copy any part of a homework. Each student must produce his/her own homework to be handed in.

Feel free to ask me for help after you have attempted the questions. The grader for the course does not have the time to provide detailed explanations on each question. To make up for this, I will try to prepare homework solutions detailed enough to allow you to understand how the question could be approached. Homework solutions will be available on the class web site.

**Exams:** There will be two midterms and one final exam. All exams will be administered **in the classroom**. The final exam will take place at the time and date established by the University. Information about the exams will be posted well in advance through the course website.

Midterm I Fri Feb 17 1:50–2:45 pm Midterm II Wed Mar 29 1:50–2:45 pm Final Tue May 2 4.00–5.45 pm

All exams are **closed book/closed notes.** There are no make-up exams. A basic calculator is allowed – tablets, laptops, and cellphones are not allowed. Statistical tables will be provided as needed.

**Homework preparation rules:** Homework may be uploaded to Carmen in PDF or Word format. PDF scans of handwritten pages are acceptable. Put your name and the homework assignment number at the top of the first page. Number all pages consecutively. Submit the problems in order.

The midterm exams will focus on the material covered most recently (since the beginning of the course for Midterm I and since Midterm I for Midterm II).

The final will cover all the material for the course.

## Late assignments

Assignments will be due at the time posted on Carmen. With few exceptions, late assignments will not be accepted.

## **Grading scale**

Final grades will be assigned based on performance in the course. The grades will not be lower than those in the "straight scale" of 90% for an A, 80% for a B, 70% for a C and so on. Appropriate adjustments to these cutoffs will be made to account for the difficulty of the exam questions.

# Faculty feedback and response time

I am providing the following list to give you an idea of my intended availability throughout the course. (Remember that you can call **614-688-HELP** at any time if you have a technical problem.)

#### Grading and feedback

For large weekly assignments, you can generally expect feedback within 7-10 days.

#### E-mail

I will reply to e-mails within 24 hours on school days.

# Attendance, participation, and discussions

The class is designed around the lectures. Attendance is strongly encouraged as is class participation. If you have questions, ask in class, or see me during office hours.

If you are unable to attend due to COVID-19 or for other reasons, let me know. If you test positive for the virus or believe that you have symptoms, it is best that you take care of health concerns before worrying about this class. Let me know of the situation promptly and we will make special arrangements.

# Other course policies

# **Health and safety**

The Ohio State University Wexner Medical Center's Cornavirus Outbreak site (<a href="https://wexnermedical.osu.edu/features/coronavirus">https://wexnermedical.osu.edu/features/coronavirus</a>) includes the latest information about COVID-19 as well as guidance for students, faculty and staff. Guidelines and requirements for campus safety from the University's Reactivation Task Force are published on the Safe and Healthy website (<a href="https://safeandhealthy.osu.edu">https://safeandhealthy.osu.edu</a>).

## Potential disruptions to instruction

- As much as possible, students will have access to material online if they are unable to attend class because of positive diagnosis, symptoms, or quarantine required following contact tracing.
- If the instructor is unable to be present in person because of positive diagnosis, symptoms, or quarantine following contact tracing a new instructor will be assigned to the course. Details will be given on the course website.

#### Student academic services

Student academic services offered on the OSU main campus <a href="http://advising.osu.edu/welcome.shtml">http://advising.osu.edu/welcome.shtml</a>.

# **Student support services**

Student support services offered on the OSU main campus:

https://artsandsciences.osu.edu/current-students/undergraduate-students/student-resources.

# **Academic integrity policy**

#### Policies for this online course

- Exams: You must complete the exams yourself, without any external help or communication.
- Written homework assignments: You are encouraged to work with fellow students on the homework, but do not copy any part of a homework. Each student must produce his/her own homework to be handed in.

#### Ohio State's academic integrity policy

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term "academic misconduct" includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct <a href="https://trustees.osu.edu/bylaws-and-rules/code">https://trustees.osu.edu/bylaws-and-rules/code</a>.

# **Copyright disclaimer**

The materials used in connection with this course may be subject to copyright protection and are only for the use of students officially enrolled in the course for the educational purposes associated with the course. Copyright law must be considered before copying, retaining, or disseminating materials outside of the course.

### Statement on title IX

Title IX makes it clear that violence and harassment based on sex and gender are Civil Rights offenses subject to the same kinds of accountability and the same kinds of support applied to offenses against other protected categories (e.g., race). If you or someone you know has been sexually harassed or assaulted, you may find the appropriate resources at <a href="http://titleix.osu.edu">http://titleix.osu.edu</a> or by contacting the Ohio State Title IX Coordinator at <a href="mailto:titleix@osu.edu">titleix@osu.edu</a>

# Accessibility accommodations for students with disabilities

The university strives to make all learning experiences as accessible as possible. In light of the current pandemic, students seeking to request COVID-related accommodations may do so through the university's request process, managed by Student Life Disability Services. If you anticipate or experience academic barriers based on your disability (including mental health, chronic, or temporary medical conditions), please let me know immediately so that we can privately discuss options. To establish reasonable accommodations, I may request that you register with Student Life Disability Services. After registration, make arrangements with me as soon as possible to discuss your accommodations so that they may be implemented in a timely fashion. SLDS contact information: <a href="mailto:slds@osu.edu">slds@osu.edu</a>; 614-292-3307; <a href="http://slds.osu.edu">http://slds.osu.edu</a>; 098 Baker Hall, 113 W. 12th Avenue.

#### Accessibility of course technology

This online course requires use of Carmen (Ohio State's learning management system) and other online communication and multimedia tools. If you need additional services to use these technologies, please request accommodations with your instructor.

- Carmen (Canvas) accessibility
- Streaming audio and video
- Synchronous course tools

#### Your mental health

As a student you may experience a range of issues that can cause barriers to learning, such as strained relationships, increased anxiety, alcohol/drug problems, feeling down, difficulty concentrating and/or lack of motivation. These mental health concerns or stressful events may lead to diminished academic performance or reduce a student's ability to participate in daily activities. The Ohio State University offers services to assist you with addressing these and other concerns you may be experiencing. If you or someone you know are suffering from any of the aforementioned conditions, you can learn more about the broad range of confidential mental health services available on campus via the Office of Student Life's Counseling and Consultation Service (CCS) by visiting <a href="ccs.osu.edu">ccs.osu.edu</a> or calling 614- 292-5766. CCS is located on the 4th Floor of the Younkin Success Center and 10th Floor of Lincoln Tower. You can reach an on call counselor when CCS is closed at 614-292-5766 and 24 hour emergency help is also available through the 24/7 National Suicide Prevention Hotline at 1-800-273- TALK or at suicidepreventionlifeline.org

# **Disclaimer**

This syllabus should be taken as a fairly reliable guide for the course content. However, you cannot claim any rights from it and in particular we reserve the right to change due dates or the methods of grading and/or assessment if necessary. Any changes will be communicated to you through official course announcements.

# **Course schedule (tentative)**

Week	Dates	Topics, Readings, Assignments, Deadlines
1	Jan 9, 11, 13	Basic elements of decision theory; Bayesian expected loss, frequentist risk, Bayes risk; Decision principles
2	Jan 18, 20	Relationship between the conditional Bayes and the Bayes risk principles; Likelihood ratio test; Sufficiency and convexity
3	Jan 23, 25, 27	Likelihood principle; Sufficiency principle; Conditionality principle; Utility theory
4	Jan 30, Feb 1, 3	Axiomatic development of utility
5	Feb 6, 8, 10	Overview of Bayesian analysis; Admissibility of Bayes rules
6	Feb 13, 15, 17	Complete class theorem
		Midterm Exam I – Fri, Feb 17, 1:50-2:45 pm
7	Feb 20, 22, 24	Minimax rules and the minimax theorem
8	Feb 27, Mar 1, 3	Generalized Bayes rules; Admissibility of generalized Bayes rules; Relationships between minimax, Bayes, and admissible rules; James-Stein estimator; Prior distributions
9	Mar 6, 8, 10	Prior distributions (continued); Empirical Bayes analysis (nonparametric and parametric)
10	Mar 20, 22, 24	Empirical Bayes for regression structures; General hierarchical models; Bayesian analysis of the linear model
11	Mar 27, 29, 31	Conditional independence and exchangeability; Finite exchangeable Bernoulli case
		Midterm Exam II – Wed, Mar 29, 1:50-2:45 pm
12	Apr 3, 5, 7	Infinite exchangeable Bernoulli case; De Finetti's theorem
13	Apr 10, 12, 14	Distinct points of view about statistical hypothesis testing; Checking Bayesian models; Bayesian model diagnostics

Week	Dates	Topics, Readings, Assignments, Deadlines
14	Apr 17, 19, 21	Bayes factors and testing; Bayesian model averaging; Bayesian model comparison
15	Apr 24	Case study analysis
16	May 2	Final Exam – Tue, May 2, 4.00-5.45 pm