SYLLABUS: STAT 7201
PROBABILITY THEORY
AUTUMN 2020

Course overview

Instructor
Instructor: Radu Herbei
Email address: herbei.1@osu.edu
Office hours: Virtual Hours via Carmen Zoom: Tuesdays 11:00-12:00am, Wednesdays, 12:00pm-1:00pm.
Office Location: CH 223.

Course description
Statistics 7201 is a measure-theoretic probability course, which introduces probability from a general and rigorous mathematical viewpoint. This course complements other courses on this topic that you may have had and will help you gain a deeper and more thorough understanding of probability and its relevance in statistics and in the real world. Students will also develop skills in constructing rigorous proofs.

Course learning outcomes
By the end of this course, students should successfully be able to:

• understand probability models from a measure-theoretic perspective
• develop rigorous proofs using advanced probability concepts.
• Connect probabilistic concepts and results to their statistical applicability.
Course materials

Required

A Probability Path by S. Resnick, Birkhauser, 2005. The book is available for download here:

Optional materials

Probability and Measure by P. Billingsley, Wiley, 1995;


Probability: Theory and Examples by R. Durrett, Duxbury Press;

Probability for Statisticians by G. Shorack, Springer.
https://link-springer-com.proxy.lib.ohio-state.edu/book/10.1007/978-3-319-52207-4

Course technology

For help with your password, university e-mail, Carmen, or any other technology issues, questions, or requests, contact the OSU IT Service Desk. Standard support hours are available at https://ocio.osu.edu/help/hours, and support for urgent issues is available 24x7.

- Self-Service and Chat support: http://ocio.osu.edu/selfservice
- Phone: 614-688-HELP (4357)
- Email: 8help@osu.edu
- TDD: 614-688-8743

Baseline technical skills necessary for online courses

- Basic computer and web-browsing skills
- Navigating Carmen

Technology skills necessary for this specific course

- CarmenZoom
- Collaborating in CarmenWiki
- Recording a slide presentation with audio narration
- Recording, editing, and uploading video
Necessary equipment

- Computer: current Mac (OS X) or PC (Windows 10+) with high-speed internet connection
- Webcam: built-in or external webcam, fully installed
- Microphone: built-in laptop or tablet mic or external microphone

Necessary software

- **Microsoft Office 365 ProPlus** All Ohio State students are now eligible for free Microsoft Office 365 ProPlus through Microsoft’s Student Advantage program. Each student can install Office on five PCs or Macs, five tablets (Windows, iPad® and Android™) and five phones.
  - Students are able to access Word, Excel, PowerPoint, Outlook and other programs, depending on platform. Users will also receive 1 TB of OneDrive for Business storage.
  - Office 365 is installed within your BuckeyeMail account. Full instructions for downloading and installation can be found [https://ocio.osu.edu/kb04733](https://ocio.osu.edu/kb04733).

Course delivery

The class meets on MWF from 10:20am – 11:15am. For the AU20 semester, the class is offered in a hybrid format. Each Monday, we will meet **in person** in Pomerene Hall room 301. On Wednesdays and Fridays, the instruction will take place asynchronously. An instructional video will be posted on Carmen ahead of time for each of these class periods. You are responsible for watching the videos and studying the material that is assigned each week. In addition to the lecture videos, weekly assignments will be posted on the class website. You will be given ample time to complete the assignments.

The instructor will hold weekly office hours via CarmenZoom as indicated above. The instructor will also initiate and manage active discussion boards, also via Carmen.

The vast majority of the course can be completed asynchronously, meaning that you will be able to study materials and work on assessments according to your own schedule.
Grading and faculty response

Grades

<table>
<thead>
<tr>
<th>Assignment or category</th>
<th>Percentage</th>
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</thead>
<tbody>
<tr>
<td>Homework</td>
<td>20%</td>
</tr>
<tr>
<td>Quizzes</td>
<td>20%</td>
</tr>
<tr>
<td>Midterm 1</td>
<td>20%</td>
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<tr>
<td>Midterm 2</td>
<td>20%</td>
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<tr>
<td>Final exam</td>
<td>20%</td>
</tr>
<tr>
<td>Total</td>
<td>100%</td>
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</tbody>
</table>

Assignment information

**Homework:** There will be weekly homework assignments posted on the course website. Homework is due once per week, with dates and times provided as needed.

**Quizzes:** There will be weekly quizzes. These will be administered online, through Carmen. There will be a sufficiently large time window, but once you begin taking the quiz there will be a time limit for you to complete it. **Proctorio** will be used during the quizzes.

**Exams:** There will be two midterm exams and one final exam. All exams will be delivered remotely, via Carmen. The final exam will take place at the time and date established by the University. Information about the exams will be posted well in advance through the course website. **Proctorio** will be used during exams.

Late assignments

Generally late assignments are not accepted, and written documentation is required for missed assignments. If you are unable to complete an assignment on time, please get in touch with me *as soon as possible* so we can discuss your situation.
Faculty feedback and response time

I am providing the following list to give you an idea of my intended availability throughout the course. (Remember that you can call 614-688-HELP at any time if you have a technical problem.)

Grading and feedback
For large weekly assignments, you can generally expect feedback within 7 days.

E-mail
I will reply to e-mails within 24 hours on school days.

Discussion board
I will check and reply to messages in the discussion boards every 24 hours on school days.

Attendance, participation, and discussions

Student participation requirements

Because this course has a significant distance-education component, your attendance is also based on your online activity and participation. The following is a summary of everyone’s expected participation:

- **Logging in: AT LEAST ONCE PER WEEK**
  Be sure you are logging in to the course in Carmen each week, including weeks with holidays or weeks with minimal online course activity. (During most weeks you will probably log in many times.) If you have a situation that might cause you to miss an entire week of class, discuss it with me as soon as possible.
• **Office hours and live sessions: OPTIONAL OR FLEXIBLE**
  All live, scheduled events for the course, including my office hours, are optional. For live presentations, I will provide a recording that you can watch later. If you are required to discuss an assignment with me, please contact me at the beginning of the week if you need a time outside my scheduled office hours.

• **Participating in discussion forums: SEVERAL TIMES PER WEEK**
  As participation, each week you can expect to post several times as part of our substantive class discussion on the week's topics.

**Discussion and communication guidelines**
The following are my expectations for how we should communicate as a class. Above all, please remember to be respectful and thoughtful.

• **Writing style:** While there is no need to participate in class discussions as if you were writing a research paper, you should remember to write using good grammar, spelling, and punctuation. Informality (including an occasional emoticon) is fine for non-academic topics.

• **Tone and civility:** Let's maintain a supportive learning community where everyone feels safe and where people can disagree amicably. Remember that sarcasm doesn't always come across online.

• **Citing your sources:** When we have academic discussions, please cite your sources to back up what you say. (For the textbook or other course materials, list at least the title and page numbers. For online sources, include a link.)

• **Backing up your work:** Consider composing your academic posts in a word processor, where you can save your work, and then copying into the Carmen discussion.

**Other course policies**

**Health and safety**
The Ohio State University Wexner Medical Center's Coronavirus Outbreak site ([https://wexnermedical.osu.edu/features/coronavirus](https://wexnermedical.osu.edu/features/coronavirus)) includes the latest information about COVID-19 as well as guidance for students, faculty and staff.

I expect that you will read and follow the guidelines and requirements for campus safety, which are available at [https://safeandhealthy.osu.edu](https://safeandhealthy.osu.edu).

**Student academic services**
Student academic services offered on the OSU main campus [http://advising.osu.edu/welcome.shtml](http://advising.osu.edu/welcome.shtml).
Student support services
Student support services offered on the OSU main campus [http://ssc.osu.edu](http://ssc.osu.edu).

Academic integrity policy

Policies for this online course

- **Quizzes and exams**: You must complete the midterm and final exams yourself, without any external help or communication.
- **Written assignments**: Your written assignments, including discussion posts, should be your own original work. You are encouraged to ask a trusted person to proofread your assignments before you turn them in—but no one else should revise or rewrite your work.
- **Reusing past work**: In general, you are prohibited in university courses from turning in work from a past class to your current class, even if you modify it. If you want to build on past research or revisit a topic you've explored in previous courses, please discuss the situation with me.
- **Falsifying research or results**: All research you will conduct in this course is intended to be a learning experience; you should never feel tempted to make your results or your library research look more successful than it was.
- **Collaboration and informal peer-review**: The course includes opportunities for collaboration with your classmates. While study groups and peer-review of major written projects is encouraged, remember that comparing answers on a quiz or assignment is not permitted. If you're unsure about a particular situation, please feel free just to ask ahead of time.

Ohio State’s academic integrity policy

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term “academic misconduct” includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct [http://studentlife.osu.edu/csc/](http://studentlife.osu.edu/csc/).

Copyright disclaimer

The materials used in connection with this course may be subject to copyright protection and are only for the use of students officially enrolled in the course for the educational purposes associated with the course. Copyright law must be considered before copying, retaining, or disseminating materials outside of the course. You must obtain my permission before sharing any of the materials associated with this course with others not enrolled in the class.
Statement on title IX
Title IX makes it clear that violence and harassment based on sex and gender are Civil Rights offenses subject to the same kinds of accountability and the same kinds of support applied to offenses against other protected categories (e.g., race). If you or someone you know has been sexually harassed or assaulted, you may find the appropriate resources at http://titleix.osu.edu or by contacting the Ohio State Title IX Coordinator, Kellie Brennan, at titleix@osu.edu

Accessibility accommodations for students with disabilities
The university strives to make all learning experiences as accessible as possible. In light of the current pandemic, students seeking to request COVID-related accommodations may do so through the university’s request process, managed by Student Life Disability Services. If you anticipate or experience academic barriers based on your disability (including mental health, chronic, or temporary medical conditions), please let me know immediately so that we can privately discuss options. To establish reasonable accommodations, I may request that you register with Student Life Disability Services. After registration, make arrangements with me as soon as possible to discuss your accommodations so that they may be implemented in a timely fashion. SLDS contact information: slds@osu.edu; 614-292-3307; http://slds.osu.edu; 098 Baker Hall, 113 W. 12th Avenue.

Accessibility of course technology
This online course requires use of Carmen (Ohio State's learning management system) and other online communication and multimedia tools. If you need additional services to use these technologies, please request accommodations with your instructor.

- Carmen (Canvas) accessibility
- Streaming audio and video
- Synchronous course tools

Your mental health
As a student you may experience a range of issues that can cause barriers to learning, such as strained relationships, increased anxiety, alcohol/drug problems, feeling down, difficulty concentrating and/or lack of motivation. These mental health concerns or stressful events may lead to diminished academic performance or reduce a student’s ability to participate in daily activities. The Ohio State University offers services to assist you with addressing these and other
concerns you may be experiencing. If you or someone you know are suffering from any of the aforementioned conditions, you can learn more about the broad range of confidential mental health services available on campus via the Office of Student Life’s Counseling and Consultation Service (CCS) by visiting ccs.osu.edu or calling 614-292-5766. CCS is located on the 4th Floor of the Younkin Success Center and 10th Floor of Lincoln Tower. You can reach an on call counselor when CCS is closed at 614-292-5766 and 24 hour emergency help is also available through the 24/7 National Suicide Prevention Hotline at 1-800-273-TALK or at suicidepreventionlifeline.org

Disclaimer
This syllabus should be taken as a fairly reliable guide for the course content. However, you cannot claim any rights from it and in particular we reserve the right to change due dates or the methods of grading and/or assessment if necessary. Any changes will be communicated to you through official course announcements.

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<thead>
<tr>
<th>Week</th>
<th>Dates</th>
<th>Topics, Readings, Assignments, Deadlines</th>
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<tbody>
<tr>
<td>1</td>
<td>8/25/20 – 8/28/20</td>
<td>Introduction, Classes of Sets</td>
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<tr>
<td>2</td>
<td>8/31/20 – 9/4/20</td>
<td>Sigma-fields, Borel sigma-fields, Induced sigma-fields</td>
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<tr>
<td>3</td>
<td>9/7/20 – 9/11/20</td>
<td>Probability measures</td>
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<tr>
<td>4</td>
<td>9/14/20 – 9/18/20</td>
<td>Pi-systems, Lambda systems, extension theorem</td>
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<tr>
<td>5</td>
<td>9/21/20 – 9/25/20</td>
<td>Inverse maps, measurability</td>
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<tr>
<td>6</td>
<td>9/28/20 – 10/2/20</td>
<td>Independence</td>
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<tr>
<td>7</td>
<td>10/5/20 – 10/9/20</td>
<td>Zero-one laws, Tail sigma-fields.</td>
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<tr>
<td>8</td>
<td>10/12/20 – 10/16/20</td>
<td>Integration, MCT, Fatou's lemma.</td>
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<tr>
<td>9</td>
<td>10/19/20 – 10/23/20</td>
<td>Radon-Nikodym’s Theorem; Conditional Expectation</td>
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<tr>
<td>10</td>
<td>10/26/20 – 10/30/20</td>
<td>Conditional Expectation; Product spaces</td>
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<tr>
<td>11</td>
<td>11/2/20 – 11/6/20</td>
<td>Convergence concepts</td>
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<tr>
<td>12</td>
<td>11/9/20 – 11/13/20</td>
<td>Laws of large numbers</td>
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<tr>
<td>13</td>
<td>11/16/20 – 11/20/20</td>
<td>Sums of independent rvs, Convergence in distribution</td>
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<tr>
<td>14</td>
<td>11/23/20 – 11/27/20</td>
<td>Convergence in distribution, CLTs</td>
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<tr>
<td>15</td>
<td>11/30/20 – 12/4/20</td>
<td>CLTs</td>
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</tbody>
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