# STAT 6860: Foundations of the Linear Model

**STAT 6860** 

#### **Course Information**

- Instructor: Yunzhang Zhu Office: 425 Cockins Hall
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  Office Hours: Monday and Wednesday 2:50 pm - 3:50 pm and by appointment (via email).
- Grader: Jiae Kim Email: kim.3887@osu.edu
- Lecture Time: Tuesday and Thursday 12:40 pm 2:30 pm, University Hall 056
- Textbook: Matrix Algebra from a Statistician's Perspective, by D. A. Harville, Springer. The Ebook is freely available for download at https://library.ohio-state.edu/record= b4801173. This text is excellent, but it was not written with a course in mind. Instead, it has been written as a reference book and it contains a wealth of useful results. This text was chosen for the course because it is one you can read with only a standard under-graduate course on linear algebra as background and because it is a great book to have on your bookshelf.
- Description: STAT 6860 is designed to get you ready for the second year course on linear model. While you have all seen linear algebra in undergraduate coursework, the typical course is taught with the goal of mathematics in mind. In Statistics, different parts of linear algebra are more important, and we will spend time on some of these areas. Particular examples include the emphasis in Statistics on covariance matrices (square, symmetric, non-negative definite), projections and successive projections as they relate to least squares fits of a model, and the ordering of matrices that is useful for optimal design. During the course, we will review basic concepts of linear algebra and we will build connections to formal statistical models and methods in particular to the multivariate normal distribution and to the linear model, as well as to least squares and related techniques.

Here is a tentative list of topics that will be covered:

- Basic notations and definitions of matrix and vector
- Column space of a matrix
- Spans, bases and ranks

- Geometric views of some matrix operations
- Matrix decomposition
- Idempotent matrices; systems of linear equations
- Projections
- Least squares
- Successive projections
- Generalized inverses
- Weighted least squares and generalized least squares
- Eigenvalues and Eigenvectors
- Prerequisites: Enrollment in the PhD program in Statistics or Biostatistics, or permission of the instructor

#### Course website

All course materials are kept on Canvas http://carmen.osu.edu.

#### Homework

Homework will be collected approximately weekly, making for about 6 homework assignments. You can work together and discuss problems, but make sure that the write-up is your own. Solutions to many of the homework problems are readily available, but finding solutions online or in printed form and copying them would constitute cheating. Please write your homework neatly, so that the TA can easily read it. A subset of problems from each assignment will be graded. Turning homework up to one day late will lead to 10% deduction from the assignment points, and no homework will be accepted more than one day late or after the solutions are available.

### Evaluation

Your final grade for this course will be determined by your performance on homework, the midterm, and final exam. The weights for each are as follows:

Homework	30~%
Midterm	30~%
Comprehensive final	40~%

### Exam schedule

There will be one midterm and one comprehensive final exam.

• The midterm will be in class, closed-book and closed-notes. It will be approximately one hour, during the second half of the class on February 6, in the lecture classroom.

- The comprehensive final exam will also be closed-book and closed-notes, with more weight on post-midterm materials. It will be on Februray 25, 12:40 pm 2:25 pm, in the lecture classroom.
- You have until one week after receiving your grades on the exams to dispute the grade; the same applies to any homework grade. Note that when asking for a question to be re-graded, the entire assignment/exam may be re-graded, and so you run the risk of losing more points than you gain back.

# Academic Integrity

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term "academic misconduct" includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct http://studentlife.osu.edu/csc/.

# **Disability Statement**

The University strives to make all learning experiences as accessible as possible. If you anticipate or experience academic barriers based on your disability (including mental health, chronic or temporary medical conditions), please let me know immediately so that we can privately discuss options. To establish reasonable accommodations, I may request that you register with Student Life Disability Services. After registration, make arrangements with me as soon as possible to discuss your accommodations so that they may be implemented in a timely fashion. SLDS contact information: slds@osu.edu; 614-292-3307; slds.osu.edu; 098 Baker Hall, 113 W. 12th Avenue.

# Disclaimer

This syllabus should be taken as a fairly reliable guide for the course content. However, you cannot claim any rights from it and in particular I reserve the right to change due dates or the methods of assessment. Official announcements will ALWAYS be those made in class.